

# Innovative Cavity Design for Hydrogen Masers using Simulation Methods

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## Abstract

The research paper aims to describe the design and improvement of a microwave cavity employed in an active hydrogen maser for use in NavIC and Deep Space Network systems. The exceptional frequency stability of the hydrogen maser depends on the behavior of hydrogen atoms within a finely tuned microwave cavity [2]. The paper explores critical factors in the design of this casing, including cavity form, material selection, and magnetic field homogeneity. These elements are essential for establishing proper resonance—the resulting frequency of the vibratory motion necessary for achieving the intended goal frequency and Q-factor.

Advanced simulation tools like HFSS and Ansys Maxwell are used for modeling the cavities. Following this, the performance of the cavities is evaluated under different operational conditions. The study focuses on the effects of these design features on the maser's stability and examines whether it is a viable technology for further development, particularly in space-related navigation systems where long-term frequency stability is crucial.

The findings contribute to the creation of more accurate and precise time sources for satellite navigation systems [4].

## Introduction

The hydrogen maser is one of the most stable sources of frequency normalization and can make significant contributions to high-precision navigation systems, including NavIC and the Deep Space Network. This device leverages the principles of quantum mechanics, utilizing hydrogen atoms to provide a consistent and accurate time signal [3].

The microwave cavity is the most critical component of the hydrogen maser, designed to resonate at the frequency corresponding to the atomic resonance of hydrogen, specifically the hyperfine transition of one of its atoms [6]. The design and optimization of this cavity are crucial for ensuring the frequency stability

and overall reliability of the maser. This research focuses on the design parameters of the microwave cavity, which shape the behavior of the system and determine its performance. These factors significantly impact the functionality of navigation systems [5].

## Design Specifications

The microwave cavity, designed cylindrically for this study, is determined by geometric measures of size or dimensions and material composition. This is vital for attaining resonance characteristics. Constructed from aluminium due to its excellent conductivity and suitability for microwave applications, the cavity operates in a vacuum environment. This setup reduces dielectric losses and keeps electromagnetic fluctuations low.

## Dimensions

The cavity has a radius  $a=135$  mm and a length  $b=370.2$ mm. These basic dimensions reflect the frequency characteristics of the cavity.

## Resonant Frequencies

In the vacuum environment, the resonant frequencies  $f_{mnp}$  for the cylindrical cavity are calculated using: for the cylindrical cavity are calculated using:

$$f_{mnp} = \frac{c}{2\pi\sqrt{\epsilon_r}} \sqrt{\left(\frac{X'_{mn}}{a}\right)^2 + \left(\frac{p\pi}{b}\right)^2}$$

is the speed of light in a vacuum (a fundamental constant of nature) [9].

$m$  and  $n$  are integers that define mode numbers along the radial and circumferential (or transverse) directions in the axial direction.

These resonant frequencies are significantly affected by the dimensions of the cavity,  $a$  and  $b$ . Small variations in these dimensions can significantly influence the frequency, emphasizing the importance of accurate dimensional control during fabrication and simulation. This accuracy is crucial for attaining the

desired operational frequencies.

### Quality Factor (Q-factor)

The quality factor Q of the cavity in which the proton beam is to be installed is determined by the level of vacuum conditions [11] and can be expressed as:

$$Q = \frac{2\pi f_{mn} \epsilon_r V}{P_{loss}}$$

V is the volume of the cavity,

P<sub>loss</sub> represents the power dissipated due to losses.

### Design Methodology

#### Hydrogen Source

Pure hydrogen gas is admitted into the maser chamber, where it is dissociated into atomic hydrogen through a process such as a radio frequency discharge.

#### Atomic Beam Formation

Hydrogen atoms are then gathered into a parallel beam passing through a magnetic state selector. This selector ensures that only atoms in a specific quantum state (usually in the low energy state) proceed further.

#### Microwave Cavity

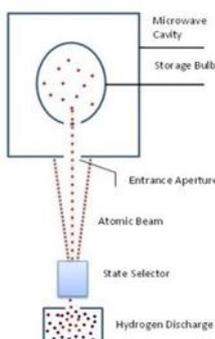
The beam of hydrogen atoms intersects a microwave cavity resonator at the hyperfine transition frequency of hydrogen (approximately 1.42 GHz). Inside the cavity, the hydrogen atoms respond directly to the microwave field [10].

#### Stimulated Emission

The interaction between the hydrogen atoms and the microwave field results in stimulated emission of radiation. This increases the “power” of the microwave signal, which is maintained at a stable frequency due to the natural properties of the hydrogen atom [8].

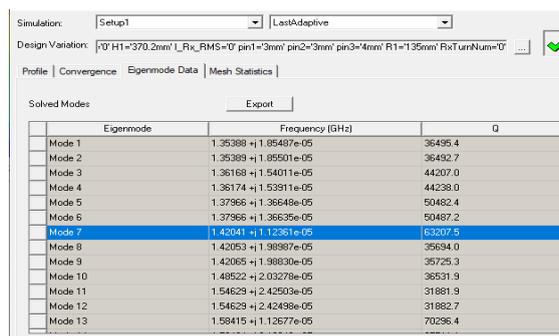
#### Feedback Loop

The emitted microwave signal is detected and used in a feedback loop to keep the system steady. This ensures constant stability and accurate phase relationships, resulting in a consistently stable and precise microwave output.



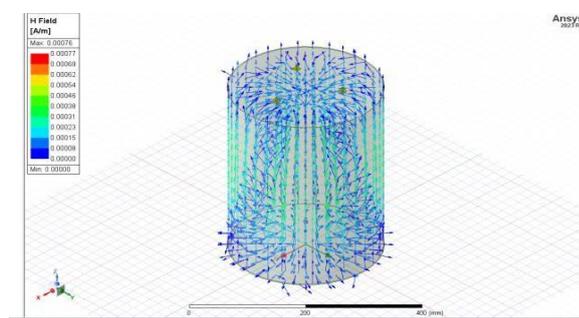
### Hydrogen Maser

### Simulation Result

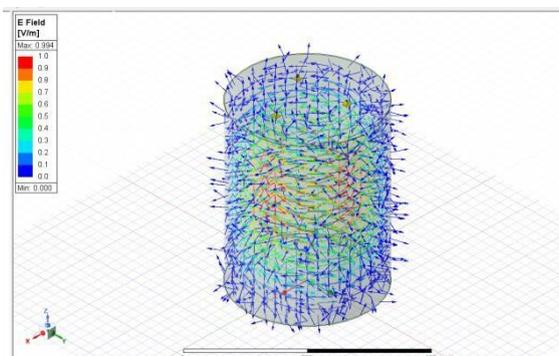


Solved Modes	Eigenmode	Frequency (GHz)	Q
Mode 1	1.35308 +j 1.85487e-05	36495.4	
Mode 2	1.35269 +j 1.85501e-05	36492.7	
Mode 3	1.36168 +j 1.54011e-05	44207.0	
Mode 4	1.36174 +j 1.53911e-05	44238.0	
Mode 5	1.37966 +j 1.36648e-05	50482.4	
Mode 6	1.37966 +j 1.36635e-05	50487.2	
Mode 7	1.42041 +j 1.12361e-05	63207.5	
Mode 8	1.42053 +j 1.98987e-05	35694.0	
Mode 9	1.42065 +j 1.98930e-05	35725.3	
Mode 10	1.48522 +j 2.03279e-05	36531.9	
Mode 11	1.54629 +j 2.42503e-05	31881.9	
Mode 12	1.54629 +j 2.42498e-05	31882.7	
Mode 13	1.58415 +j 1.12677e-05	70296.4	

Eigen Mode



Aluminium Cavity Probe H Vector



Aluminium Cavity Probe E Vector

### Result Cavity Dimensions

The cyclic cavity was modeled with dimensions of two distances:  $a=135$  mm (radius) and  $b=370.2$  mm (length), reflecting precise manufacturing specifications.

### Resonant Frequency

The simulated resonant frequency of the cavity [7] was computed by varying the length of the cavity. For the  $m=0$  and  $n=1$  modes, the resonant frequency  $fTE011$  was realized at 1.42040575177 GHz.

### Frequency Deviation

The deviation obtained shows that EMI changes by  $\Delta f=43.99$  Hz, as compared to the theoretical resonant frequency expectations.

## Quality Factor (Q-factor)

The simulation also assessed the quality factor  $Q$  of the resonator circuit. It was found that the cavity could sustain resonance with a small degree of dimensional stability loss while still maintaining the ability to transmit heat with limited energy loss. With the calculated  $Q$  factor, it is possible to move forward with confidence and strengthen existing market positions. The cavity's ability to sustain resonance and productivity in terms of frequencies over time is crucial.

## Conclusion

These results reinforce the understanding of the importance of dimensional precision in achieving the desired resonance frequency, particularly for hydrogen masers. The observed frequency deviation provides valuable insights for fine-tuning cavity dimensions, further SMA connector analysis, and the optimization of parameter values and overall effectiveness.

## Future Considerations

Further refinements under this category include costs related to controlling manufacturing methods to avoid dimensional fluctuations and improve stability rates. The emissions exhibit different forms and increased stability. Validation through simulation modifies and generalizes the results. By combining experimental findings from audited organizations and measuring their internal control levels, it is possible to compare these with internal control levels in other organizations with similar conditions.

## Acknowledgements

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